

# Implementation and Sensorless Vector-Control Design and Tuning Strategy for SMPM Machines in Fan-Type Applications

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**Abstract**—This paper presents a complete design methodology for the sensorless vector control of permanent-magnet synchronous machine (PMSM) motor drives in fan-type applications. The proposed strategy is built over a linear asymptotic state observer used to estimate the PMSM back EMF and a novel tracking controller based on a phase-locked loop system, which, by synchronizing the estimated and actual  $d-q$  frames, estimates the rotor speed and position. This paper presents the complete derivation of all associated control loops, namely, state observer; tracking controller;  $d-q$ -axis current regulator; speed controller; an antisaturation control loop, which provides inherent operation in the flux-weakening region; and all corresponding antiwindup loops. Detailed design rules are provided for each of these loops, respectively verified through time-domain simulations, frequency-response analysis, and experimental results using a three-phase 7.5-kW PMSM motor drive, validating both the design methodology and the expected performance attained by the proposed control strategy.

**Index Terms**—Luenberger observer, sensorless, SMPM, vector control.

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## I. INTRODUCTION

PERMANENT-MAGNET synchronous machines (PMSMs) are controlled by using the rotor position information to synchronize the machine line currents and their sinusoidal back EMF. The rotor position may be obtained using resolvers or encoders depending on the level of accuracy required by the application. Regardless of this choice, these position transducers have inherent disadvantages, such as a reduced reliability due to their sensitivity to vibration, humidity corrosive refrigerants, high temperature, and electromagnetic noise, as well as increased costs, weight, and volume. For these reasons, the sensorless control of PMSM has become increasingly attractive.

The sensorless control for these permanent-magnet (PM) machines can be divided into two categories, one based on the back-EMF estimation and the other based on the saliency phenomena of the machine. While the former strategies reveal good performance in the high-speed region, they fail in the low-speed region and simply cannot operate at zero speed, as opposed to the latter strategies which can operate in the low-speed region including standstill. The tradeoff for using these latter strategies is a higher overall complexity and much higher digital processing needs. Nonetheless, for applications operating at higher speed (typically above 0.1 p.u. of rated speed) with centrifugal-like load torque profiles, the usage of back-EMF-based estimation strategies becomes a preferred choice [1]–[8]. Accordingly, this paper addresses the sensorless vector control of fan-type applications for climate control systems.

Numerous methods have been presented so far in order to estimate the rotor position and speed of PM machines, namely, voltage integration [2], state observer including mechanical system [3], nonlinear observer [4], extended Kalman filter [5], state observer in stationary reference frame [6], and state observer in rotor reference frame [7]. All of these but [5] use a two-stage approach, i.e., they estimate the back EMF and, from it, the rotor position and speed. The advantage of this indirect approach is the greater flexibility attained to tune the estimator and PMSM speed control system; however, until now, none of this has been truly exploited, and as a result, frequency-response-based design methodologies for sensorless vector controls are hard to find for this type of motor drive.

Accordingly, this paper presents the complete design methodology for a PMSM sensorless vector control scheme using a two-stage approach. Specifically, it employs a linear

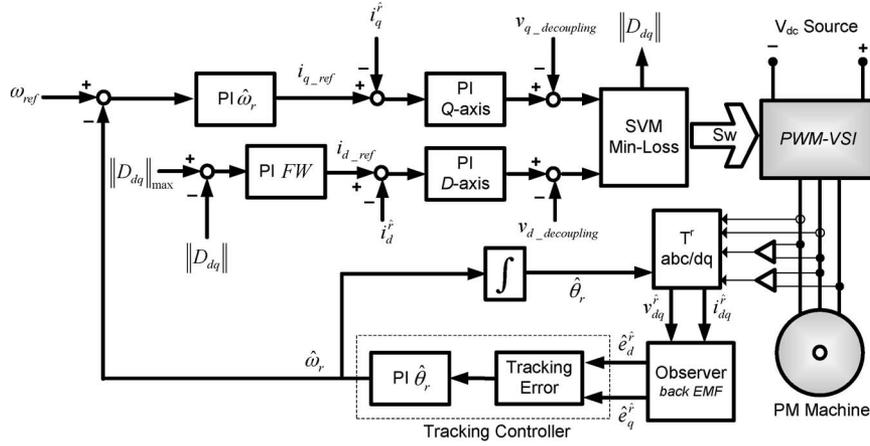


Fig. 1. Sensorless vector control scheme employed.

asymptotic state observer to estimate the machine back EMF and a tracking controller to generate the estimated speed and rotor position, the latter implemented by means of a synchronous  $d$ - $q$  frame phase-locked loop (PLL) system. Vector control is implemented over the estimation engine using a decoupled  $d$ - $q$  frame current regulator and an optimized speed-loop response covering both constant-torque and constant-power regions, where an antisaturation controller provides transparent access into the flux-weakening region of the PM machine. A detailed design procedure is provided for the proposed sensorless control strategy and verified using simulations and experimental results obtained with a 7.5-kW PMSM pulsewidth modulation (PWM) motor drive controlled using a DSP digital control system.

## II. SENSORLESS VECTOR CONTROL STRATEGY

The proposed strategy employs a linear asymptotic observer to estimate the back-EMF voltages in the rotor  $d$ - $q$  reference frame. These estimated quantities determine, with their relative magnitudes, the rotor position error of the machine, i.e., the angular difference between the actual and estimated  $d$ - $q$  frames. This error information may be readily employed under a closed-loop scheme by feeding it to the tracking controller whose output corresponds to the estimated speed of the machine, thus accelerating or decelerating the estimated  $d$ - $q$  frame speed in order to synchronize it with the actual frame. This estimated speed is then used to close the motor-drive speed loop and its integral—corresponding to the rotor position—used in all transformations between the  $abc$  and  $d$ - $q$  frames. This control structure is shown in Fig. 1, also depicting the  $d$ - $q$ -axis current regulator and flux-weakening controller.

## III. STARTING PROCEDURE

A startup procedure is mandatory for the proposed sensorless control strategy due to its dependence on the back-EMF estimation [1]. The speed range spanning from standstill to nominal speed has been divided into four operating regions as shown in Fig. 2. *Region 1* is used to align the machine; *Region 2* accelerates the machine in speed open loop while current loop

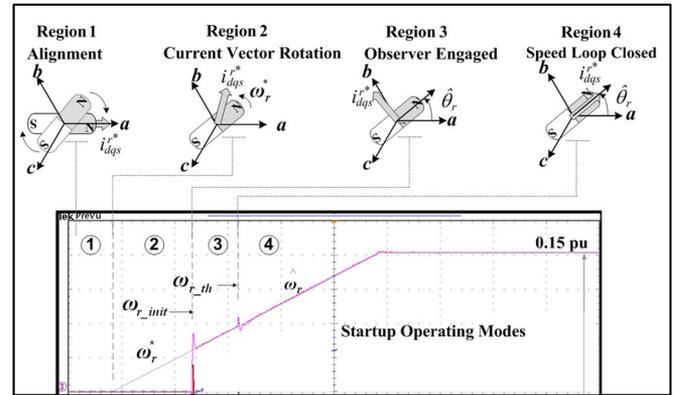


Fig. 2. Experimental result: Starting sequence employed for the proposed sensorless control strategy.

is closed; in *Region 3*, the state observer and tracking controller are engaged after passing a predefined rotor velocity value  $\omega_{r\_init}$ ; and in *Region 4*, the speed loop is closed around the threshold velocity  $\omega_{r\_th}$  after the estimated speed and rotor position values have converged, finally engaging the sensorless vector control algorithm. The value of the initial speed  $\omega_{r\_init}$ , for engaging the observer, is given as follows:

$$\omega_{r\_init} \lambda_m \geq \frac{T_{\text{deadtime}}}{T_{\text{switching}}} V_{\text{dc}} \quad (1)$$

where  $\lambda_m$  is the peak flux linkage of a phase,  $T_{\text{deadtime}}$  is the inverter dead-time delay,  $T_{\text{switching}}$  is the inverse of the switching frequency of the inverter, and  $V_{\text{dc}}$  is the inverter dc-link voltage.

At very low speed of operation (less than 0.1 p.u.) and under no load condition, the stator resistive drop and the inductive voltage drop in the motor being very small can be ignored. Then, the back-EMF voltage equals the average of the inverter output voltage, and the corresponding relation is given in (1). While (1) should be taken as a preliminary guideline, it is imperative to evaluate the lower limit for initial speed  $\omega_{r\_init}$  for individual cases and starting conditions in specific applications. In order to determine the threshold speed  $\omega_{r\_th}$ , the convergence time of the rotor position and speed estimation algorithm should be considered. Alternatively, the difference

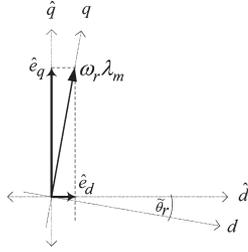


Fig. 3. Relationship between the actual and the estimated synchronous reference frames, depicting angular misalignment  $\tilde{\theta}_r$ .

between the frequency of current vector and the estimated rotor speed can be used. The initial and threshold speeds chosen in this work are 0.05 and 0.08 p.u. of the rated speed, respectively.

#### IV. STATE EQUATIONS IN ESTIMATED REFERENCE FRAME

The voltage equations for SMPM machines in the actual rotor reference frame can be expressed as

$$\begin{bmatrix} v_{ds}^r \\ v_{qs}^r \end{bmatrix} = \begin{bmatrix} R_s & -\omega_r L_s \\ \omega_r L_s & R_s \end{bmatrix} \begin{bmatrix} i_{ds}^r \\ i_{qs}^r \end{bmatrix} + L_s \frac{d}{dt} \begin{bmatrix} i_{ds}^r \\ i_{qs}^r \end{bmatrix} + \omega_r \lambda_m \begin{bmatrix} 0 \\ 1 \end{bmatrix} \quad (2)$$

where  $v_{qs}^r$  and  $v_{ds}^r$  are the applied stator phase voltages in rotor reference frame, while  $i_{qs}^r$  and  $i_{ds}^r$  are the corresponding currents in the stator,  $\omega_r$  is the electrical angular velocity of the rotor,  $R_s$  the per-phase stator resistance, and  $L_s$  is the per-phase stator self-inductance.

Since the real speed is not known, an alternative model is required, where the estimated rotor speed and position surrogate the real quantities. Fig. 3 shows the relationship existent between the estimated and actual  $d$ - $q$  frames, where the top hat  $\hat{\cdot}$  stands for estimated variables. The relative angular error between both frames is defined as

$$\tilde{\theta}_r \equiv \theta_r - \hat{\theta}_r \quad (3)$$

from which a geometrical relationship can be established, relating the estimated back EMF ( $\hat{e}_d^r$  and  $\hat{e}_q^r$ ) and the actual rotor speed  $\omega_r$  as follows:

$$\hat{e}_d = \omega_r \lambda_m \sin \tilde{\theta}_r \quad \hat{e}_q = \omega_r \lambda_m \cos \tilde{\theta}_r. \quad (4)$$

These relations show that, when the error between reference frames is zero, the machine back EMF on the  $q$ -axis will equal  $\omega_r \lambda_m$  as can be easily observed from Fig. 3.

The PM machine voltage (2) may accordingly be rewritten in the estimated rotor reference frame as shown in the following:

$$\begin{bmatrix} v_{ds}^{\hat{r}} \\ v_{qs}^{\hat{r}} \end{bmatrix} = \begin{bmatrix} R_s & -\hat{\omega}_r L_s \\ \hat{\omega}_r L_s & R_s \end{bmatrix} \begin{bmatrix} i_{ds}^{\hat{r}} \\ i_{qs}^{\hat{r}} \end{bmatrix} + L_s \frac{d}{dt} \begin{bmatrix} i_{ds}^{\hat{r}} \\ i_{qs}^{\hat{r}} \end{bmatrix} + \begin{bmatrix} -\hat{e}_d^r \\ \hat{e}_q^r \end{bmatrix}. \quad (5)$$

The back-EMF terms  $\hat{e}_d^r$  and  $\hat{e}_q^r$  are, however, neither state variables nor inputs to the system; therefore, in order to construct an appropriate state-space model, these variables need to be advanced to state variable status. This is possible by making the following assumption: that the rotor speed and position

remain constant during a control cycle (switching period), which is true since the sampling period is significantly smaller compared to the mechanical time constants. It follows then that

$$\dot{\hat{e}}_d = 0 \quad \dot{\hat{e}}_q = 0. \quad (6)$$

With (6), the new augmented state-space model may be readily constructed as shown in the following:

$$\dot{\mathbf{x}} = \mathbf{A}\mathbf{x} + \mathbf{B}\mathbf{u} \quad \mathbf{y} = \mathbf{C}\mathbf{x} \quad (7)$$

with

$$\begin{aligned} \mathbf{x} &= [i_{ds}^{\hat{r}} \quad i_{qs}^{\hat{r}} \quad e_d^{\hat{r}} \quad e_q^{\hat{r}}]^T \\ \mathbf{u} &= [v_{ds}^{\hat{r}} \quad v_{qs}^{\hat{r}}]^T \quad \mathbf{y} = [i_{ds}^{\hat{r}} \quad i_{qs}^{\hat{r}}]^T \\ \mathbf{A} &= \begin{bmatrix} -\frac{R_s}{L_s} & \hat{\omega}_r & \frac{1}{L_s} & 0 \\ -\hat{\omega}_r & -\frac{R_s}{L_s} & 0 & -\frac{1}{L_s} \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} \\ \mathbf{B} &= \begin{bmatrix} \frac{1}{L_s} & 0 \\ 0 & \frac{1}{L_s} \\ 0 & 0 \\ 0 & 0 \end{bmatrix} \quad \mathbf{C} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}. \end{aligned} \quad (8)$$

#### V. LINEAR ASYMPTOTIC STATE OBSERVER

The proposed sensorless control strategy employs a linear asymptotic state observer per Bertram's original introduction in 1961 [9], [10], having, as main feature, the use of feedback to drive the estimation error to zero. The estimator has the following form:

$$\dot{\hat{\mathbf{x}}} = \mathbf{A}\hat{\mathbf{x}} + \mathbf{B}\mathbf{u} + \mathbf{L}(\mathbf{y} - \mathbf{C}\hat{\mathbf{x}}) \quad (9)$$

where  $\mathbf{L}$ , defined as

$$\mathbf{L} = \begin{bmatrix} l_{11} & l_{21} & l_{31} & l_{41} \\ l_{12} & l_{22} & l_{32} & l_{42} \end{bmatrix}^T \quad (10)$$

is the feedback gain matrix that determines the exponential state error dynamics described by

$$\dot{\tilde{\mathbf{x}}} = \dot{\mathbf{x}} - \hat{\mathbf{x}} = (\mathbf{A} - \mathbf{L}\mathbf{C})\tilde{\mathbf{x}} \quad (11)$$

with  $\tilde{\mathbf{x}}(0) = \mathbf{x}_0 - \hat{\mathbf{x}}_0$ . The eigenvalues of matrix  $(\mathbf{A} - \mathbf{L}\mathbf{C})$  in (11) correspond to the natural frequencies of the observer dynamics. Therefrom, the gain values of matrix  $\mathbf{L}$  may be found by equalizing terms with the following characteristic equation:

$$\det(s\mathbf{I} - \mathbf{A} + \mathbf{L}\mathbf{C}) = C_o(s) = s^4 + a_1 s^3 + a_2 s^2 + a_3 s + a_4. \quad (12)$$

Since the PM machine model is an orthogonal system built over the  $d$ - $q$ -axes, (12) may be simplified as follows:

$$C_o(s) = (s^2 + 2\zeta\omega_o s + \omega_o^2)^2. \quad (13)$$

Then, by simple inspection of (7) and (8), the gains of matrix  $\mathbf{L}$  may be readily determined. First, the decoupled  $d$ - $q$ -axis



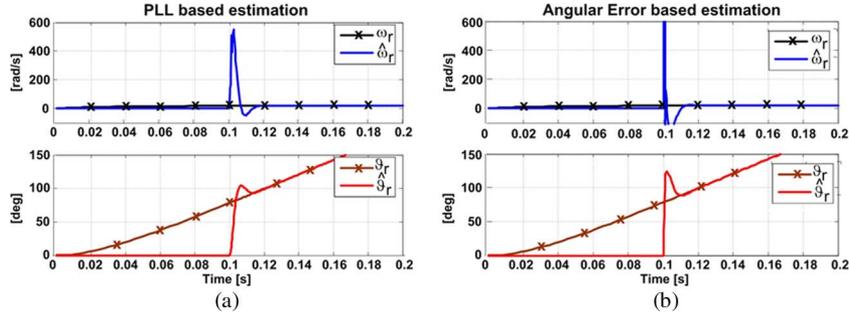


Fig. 7. Simulation results: comparison of the tracking controller schemes implemented. (a) PLL-based estimation. (b) Angular-error-based estimation.

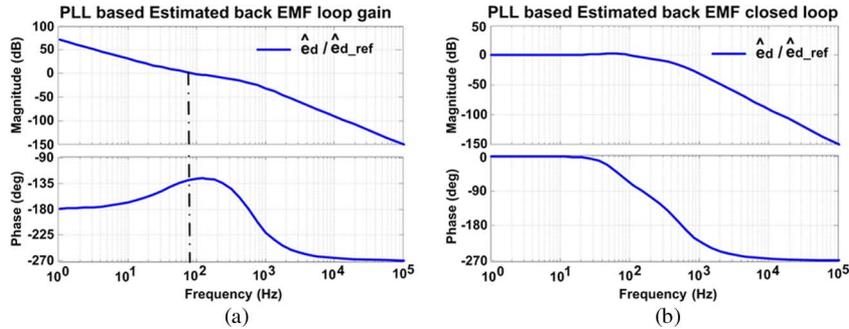


Fig. 8. Simulation results: frequency response of the PLL-based estimation technique. (a) Loop gain. (b) Closed-loop transfer function.

## VI. TRACKING CONTROLLER

A tracking controller estimates the speed and position of the machine based on the angular error [11]. This error is deduced from (4) as

$$\tilde{\theta}_r = \text{atan} \left( \frac{\hat{e}_d^r}{\hat{e}_q^r} \right). \quad (16)$$

This is a commonly used technique in sensorless control applications; however, it introduces a nonlinearity into the system and requires the usage of the inverse trigonometric function  $\text{atan}(\cdot)$ . To avoid this, an alternative tracking controller is implemented using a PLL to synchronize the estimated  $d$ - $q$  frame to the actual  $d$ - $q$  frame. This is achieved simply by regulating the  $d$ -axis back-EMF component  $\hat{e}_d^r$  to zero (Fig. 3). Fig. 6 shows the PLL-based tracking controller scheme, where  $\hat{e}_d^r$  is fed back in a closed-loop fashion using zero as reference—hence, the alignment—and a PI regulator is used to generate the estimated rotor speed  $\hat{\omega}_r$ . The estimated rotor position  $\hat{\theta}_r$  is consecutively obtained through the integration of  $\hat{\omega}_r$ .

Fig. 6 also shows the use state feedback linearization—by means of gain  $G_{\text{lin}}$ —thus ensuring a constant linear dynamic response of the tracking controller regardless of the PMSM rotor speed. This linearization gain is defined by

$$G_{\text{lin}} = \frac{-1}{\sqrt{\hat{e}_d^2 + \hat{e}_q^2}}. \quad (17)$$

The resultant closed-loop response of the tracking controller after linearization is then the following one:

$$\frac{\hat{e}_d^r(s)}{e_{d\_ref}^r(s)} = \frac{k_{pt}s + k_{it}}{s^2 + k_{pt}s + k_{it}}. \quad (18)$$

The gains of the tracking controller  $k_{pt}$  and  $k_{it}$  are then determined by setting the desired closed-loop response according to the following second-order polynomial:

$$s^2 + 2\zeta\omega_t s + \omega_t^2 \quad (19)$$

which yields the following proportional and integrative gains:

$$k_{pt} = 2\zeta\omega_t \quad k_{it} = \omega_t^2. \quad (20)$$

Fig. 7(a) shows the actual and estimated rotor speed and rotor position depicting the PLL-based tracking controller response once the state observer is enabled at time  $t = 0.1$  s. The figure shows the anticipated alignment achieved by the proposed strategy, showing a slight overshoot in correspondence with its damping coefficient selection. Fig. 7(b) similarly shows the actual and estimated rotor speed and rotor position obtained with the angular-error-based tracking controller using (16) [11]. Just as in the previous case, the state observer is enabled at time  $t = 0.1$  s, where, now, a much faster response with an overshoot twice as high as for the PLL-based tracking controller is observed, clearly not in compliance with the design specifications.

The aforementioned dynamic response is verified in Fig. 8, which shows the frequency response obtained with the PLL-based tracking controller. Fig. 8(a) shows the controller loop gain with a crossover frequency of 60 Hz, in correspondence with the design specifications, and Fig. 8(b) shows the closed-loop response depicting its resonant peak at 60 Hz.

## VII. VECTOR CONTROL STRATEGY

### A. Current Controller

Fig. 9 shows the structure of the  $d$ - $q$ -axis current regulator used. Both channels employ a PI controller with additional

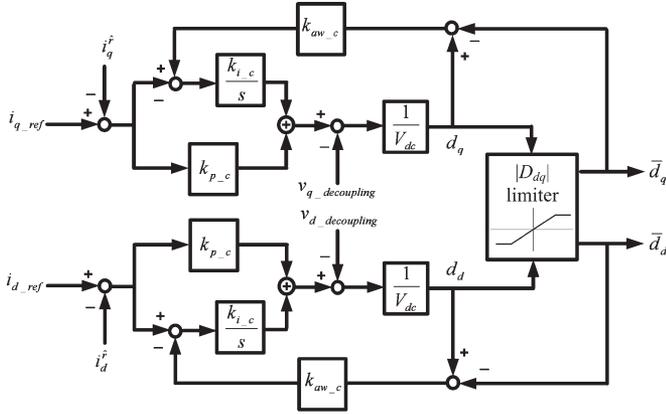


Fig. 9. PI controller implementation for  $d$ - $q$ -axis current loop including antiwindup protection using a duty-cycle  $d$ - $q$  modulus limiter.

decoupling terms used to cancel out the dynamic interactions between them. These are defined as

$$v_{d\_decoupling} = -\hat{\omega}_r L_s i_{qs}^{\hat{r}} \quad (21)$$

$$v_{q\_decoupling} = \hat{\omega}_r L_s i_{ds}^{\hat{r}} + \hat{\omega}_r \lambda_m. \quad (22)$$

The resultant ac dynamics are then simply given by

$$v_{ds}^{\hat{r}} = R_s i_{ds}^{\hat{r}} + L_s \frac{d}{dt} i_{ds}^{\hat{r}} \quad (23)$$

$$v_{qs}^{\hat{r}} = R_s i_{qs}^{\hat{r}} + L_s \frac{d}{dt} i_{qs}^{\hat{r}}. \quad (24)$$

Then, if the PI gains  $k_{p\_c}$  and  $k_{i\_c}$  are made proportional to the desired closed-loop bandwidth  $\omega_c$

$$k_{p\_c} = L_s \omega_c \quad k_{i\_c} = R_s \omega_c \quad (25)$$

the closed-loop transfer functions for both  $d$ - $q$ -axis current loops may be derived using Fig. 9 and (23) and (24)—converted into the  $s$ -domain. These are given by

$$\frac{i_{ds}^{\hat{r}}(s)}{i_{ds\_ref}(s)} = \frac{i_{qs}^{\hat{r}}(s)}{i_{qs\_ref}(s)} = \frac{\omega_c}{s + \omega_c}. \quad (26)$$

The bandwidth of  $d$ - $q$ -axis current regulator is defined as 50 times that of the speed control loop; hence,

$$\omega_c = 50 \cdot \omega_s. \quad (27)$$

The antiwindup scheme used is presented in [12], where the antiwindup gain is defined as

$$k_{aw\_c} = \frac{k_{i\_c}}{k_{p\_c}} \quad (28)$$

and both PI gains must comply with

$$k_{p\_c} \geq R_s \quad k_{i\_c} \leq \frac{k_{p\_c}^2}{(1 + \sqrt{2}) L_s}. \quad (29)$$

### B. Speed Controller

Fig. 10(a) shows a conventional closed-loop speed control scheme for PM machines. The open-loop and closed-loop

transfer functions derived from Fig. 10 are given by

$$G_{s\_ol}(s) = \frac{k_{p\_s} s + k_{i\_s} K_T P}{s J_m s^2} \quad (30)$$

$$G_{s\_cl}(s) = \frac{K_T P}{2 J_m s^2 + (k_{p\_s} s + k_{i\_s}) \frac{K_T P}{2}}. \quad (31)$$

The motor-drive mechanical dynamics are given by

$$J_m \frac{d}{dt} \omega_r + B_m \omega_r = \frac{P}{2} (T_e - T_L) \quad (32)$$

where all constants are defined in the Appendix.

In order to improve the transient performance of the speed loop, a filter precompensator is added to cancel out the zero introduced by the speed-loop PI as shown in Fig. 10(b). This prefilter is defined as

$$G_{s\_f}(s) = \frac{k_{i\_s}}{k_{p\_s} s + k_{i\_s}}. \quad (33)$$

The PI regulator and filter precompensator parameters are then defined as

$$k_{p\_s} = 2\zeta \omega_s \cdot \frac{2J_m}{K_T P} \quad k_{i\_s} = \omega_s^2 \cdot \frac{2J_m}{K_T P}. \quad (34)$$

This results in the following second-order closed-loop dynamics for the motor-drive speed loop:

$$G_{s\_cl}(s) = \frac{\omega_r(s)}{\omega_{r\_ref}(s)} = \frac{\omega_s^2}{s^2 + 2\zeta \omega_s s + \omega_s^2}. \quad (35)$$

As shown in Fig. 10(b), this control loop also employs an antiwindup scheme, with its gain defined as

$$k_{aw\_s} = \frac{k_{i\_s}}{k_{p\_s}}. \quad (36)$$

In order to ensure operation within the linear range of the closed-loop system, the PI gains should be limited to the following values per [12]:

$$k_{p\_s} \geq B_m \quad k_{i\_s} \leq \frac{k_{p\_s}^2}{(1 + \sqrt{2}) J_m}. \quad (37)$$

These restrictions provide a lower boundary for the speed-loop damping coefficient, which may be found by replacing (34) into (37) as shown in the following:

$$\zeta^2 \geq \frac{K_T P}{8} (1 + \sqrt{2}). \quad (38)$$

### C. Flux-Weakening Controller

Many different strategies have been developed for the flux-weakening control of PM machines; this paper presents an approach based on [13]. The operation beyond the machine base speed requires the PWM inverter to provide output voltages higher than its output capability—limited by its dc-link voltage—which in turn saturates the motor-drive control system if no precautions are taken. The absolute maximum duty cycle corresponding to the inverter voltage vector is defined as  $\|D_{dq}\|$ . By simple inspection of the machine model, it may



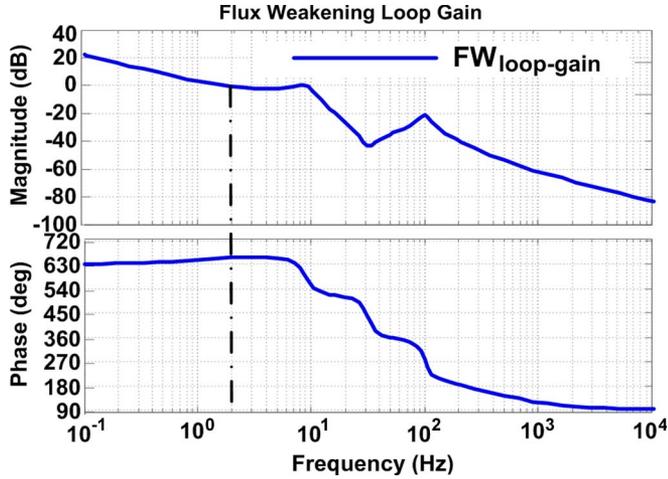


Fig. 12. Simulation result: Loop gain of the proposed antisaturation flux-weakening controller.

TABLE I  
SENSORLESS VECTOR CONTROL BANDWIDTHS

Control Loop	Symbol	Value [p.u.]
Speed Controller	$\omega_s$	1
Current Controller	$\omega_c$	50
Flux weakening controller	$\omega_{fw}$	0.75
Tracking controller	$\omega_t$	20
State observer	$\omega_o$	200

Fig. 12 shows the frequency response of the proposed antisaturation flux-weakening controller, depicting the loop-gain Bode plot and how the cutoff frequency of 2.25 Hz is effectively attained (given the 3-Hz speed-loop bandwidth).

VIII. EXPERIMENTAL RESULTS

Table I summarizes the design bandwidths for each of the control loops of the proposed strategy, which, for the previous design example ( $\omega_s = 3$  Hz), defined the following bandwidths for the current controller, flux weakening, tracking controller, and state observer: 150, 2.25, 60, and 600 Hz.

The dynamometer setup used in this work is shown in Fig. 13. It comprises a four-quadrant 10-kW motor drive on the load side and a 7.5-kW motor drive on the test side. The two systems are coupled with an HBM MP60 torque and speed transducer. An N4L PSM 1600 frequency-response analyzer is used for generating the loop gain plots. The injection signal amplitude for loop gain plots was limited to 0.05 p.u. Experimental verification of the attained bandwidth for each control loop is presented in the time and frequency domains in the following subsections.

A. Back-EMF State Observer

Fig. 14(a) shows the startup sequence of the machine and corresponding operation of the state observer in speed closed loop. The reference speed  $\omega_r^*$  was set at 0.15 p.u. that corresponds to an electrical frequency of 30 Hz. As explained in Section III, the initial and the threshold speeds were set at 0.05 and 0.08 p.u., respectively.

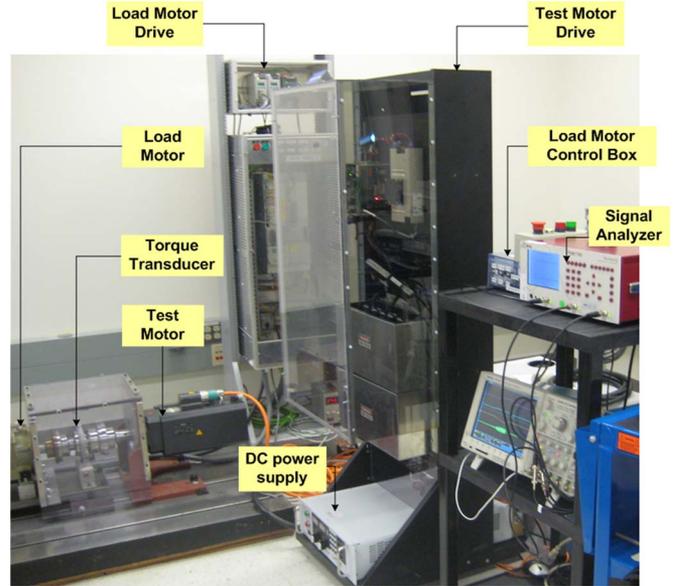


Fig. 13. Experimental setup for the validation of sensorless vector control.

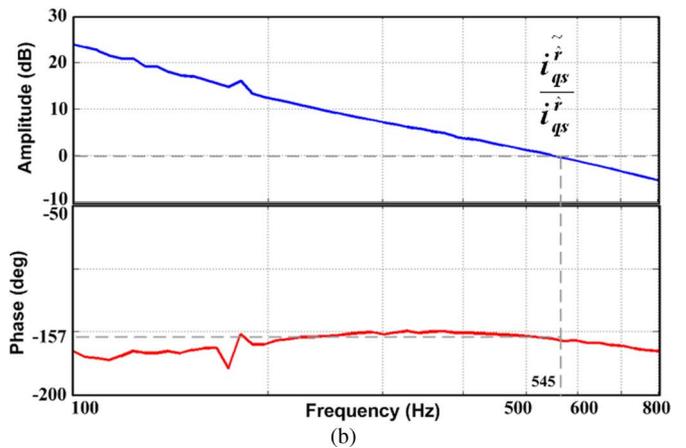
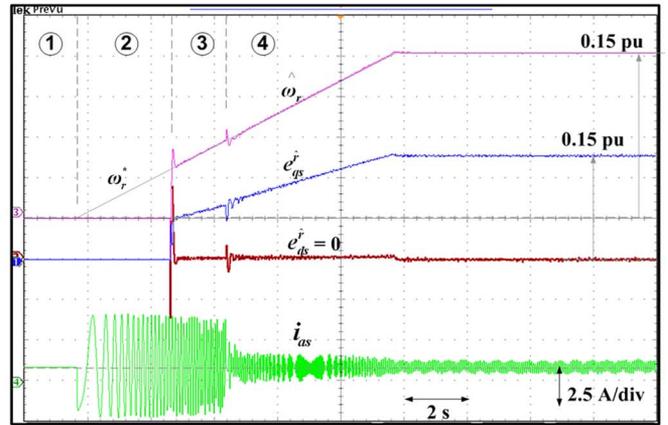


Fig. 14. Experimental results. (a) Machine startup operation under no load highlighting reference and estimated speed,  $q$ - and  $d$ -axis estimated back EMF, and phase current. (b) State observer open-loop gain highlighting the ratio of the estimated  $q$ -axis current error to the observer estimated current.

The observer is enabled in *Region 3* once the machine has left standstill and passed the prespecified initial speed. After being enabled, the estimated  $d$ - and  $q$ -axis back EMFs rapidly

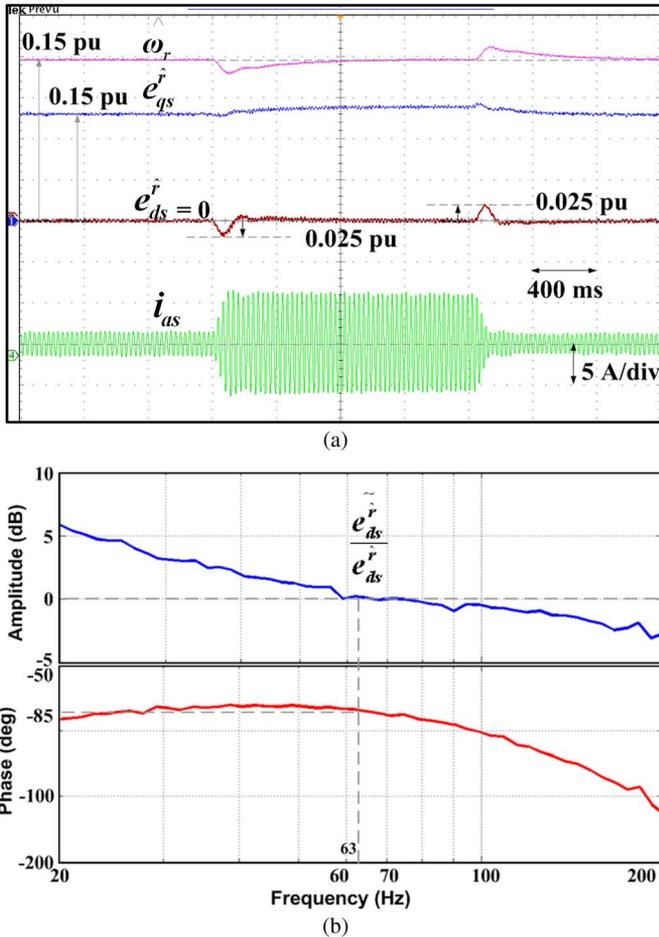


Fig. 15. Experimental results. (a) Operation with 50% step change in load torque highlighting estimated speed,  $q$ - and  $d$ -axis estimated back EMF, and phase current. (b) Tracking controller open-loop gain highlighting ratio of estimated  $d$ -axis back-EMF error to the estimated  $d$ -axis back EMF.

converge to their estimated values as shown in Fig. 14(a). When the reference speed equals the predefined threshold speed, the speed loop is closed, and, at the same time, the reference currents are switched from their open-loop predefined values to the corresponding speed and antisaturation regulator outputs; hence, the sudden drop in the phase current at the onset of *Region 4* occurs. It should be noted that, in case of full position sensor feedback closed-loop vector control, the  $q$ - and  $d$ -axis back-EMF voltages follow the linear relation  $e_{qs} = \omega_r \lambda_m$ , while  $e_{ds} = 0$ . Although some deviation from the aforementioned condition is seen during acceleration in sensorless mode of operation, the relationship is satisfied during steady state and is seen in *Region 4*. Fig. 14(b) shows the state observer open-loop gain as the ratio of estimated  $q$ -axis current error to the observer estimated current. The gain crossover frequency is 545 Hz, and the corresponding phase margin at this frequency is 23°. The distortion in the frequency response at 180 Hz is due to the inverter dead time which induces a sixth-harmonic frequency component in the estimated  $d$ - and  $q$ -axis currents. This effect can be minimized by applying dead-time compensation algorithm. It should also be mentioned that the motor back EMF is devoid of higher ordered harmonics and is purely sinusoidal. Observers with a nonsinusoidal back

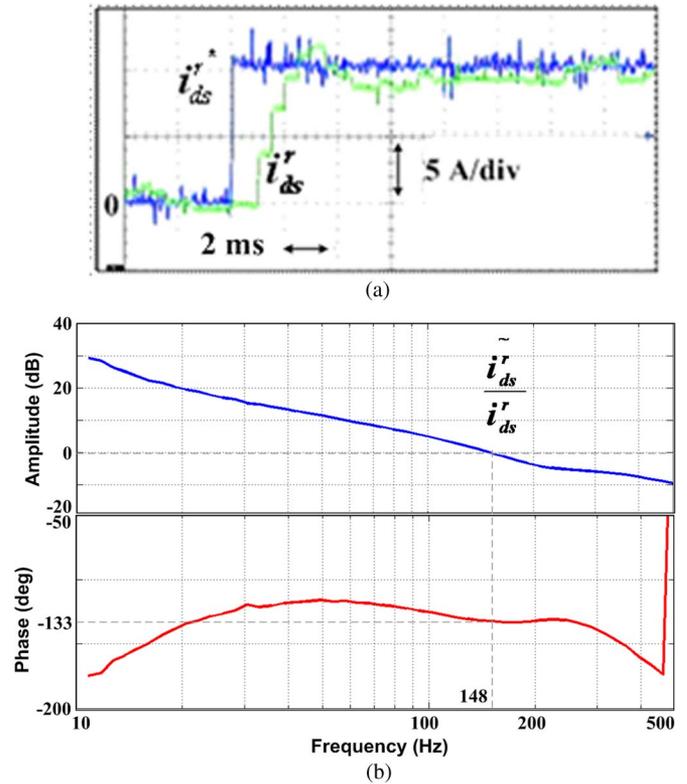


Fig. 16. Experimental results. (a) Stator  $d$ -axis current transient operation 0–10-A step change in reference and measured currents. (b) Current controller open-loop gain highlighting ratio of  $d$ -axis current error to the measured  $d$ -axis current.

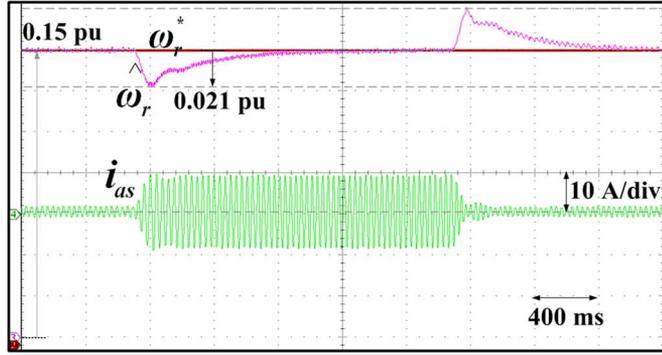
EMF must be evaluated separately and is beyond the scope of this work.

As explained in Section V, in a two-stage approach, it is essential to have the appropriate time scale separation between the back-EMF observer and the tracking controller; accordingly, the combined performance along with speed controller will be discussed in the next subsection.

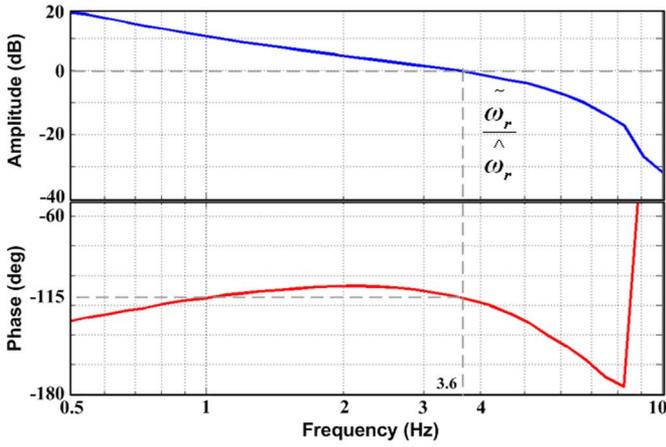
### B. Tracking Controller

Once the state observer operation is verified, the tracking controller may be readily tuned since its inputs correspond to the state observer outputs, i.e., the estimated  $d$ - $q$ -axis back EMFs.

Fig. 15(a) shows the transient response of the speed and tracking controller to a 50% step change in load torque. As seen in Fig. 15(a), the controller depicts stable operation with estimated  $d$ -axis back EMF regulated to zero and with an undershoot of 2.5% for the step load. It can be seen that the estimated speed has a dynamic response which is much slower than the estimated  $d$ -axis back-EMF voltage. It can be noted that the phase current follows the tracking observer dynamics because the output of the tracking controller is the estimated speed and position which is used for the sensorless vector control. Fig. 15(b) shows the tracking controller open-loop gain highlighting ratio of estimated  $d$ -axis back-EMF error to the estimated  $d$ -axis back EMF. The gain crossover frequency is 63 Hz. The corresponding phase margin at this frequency is 95°.



(a)



(b)

Fig. 17. Experimental results. (a) Machine transient operation with 75% step change in load torque highlighting estimated speed and reference speed and phase current. (b) Speed controller open-loop gain highlighting the ratio of speed error to the estimated speed.

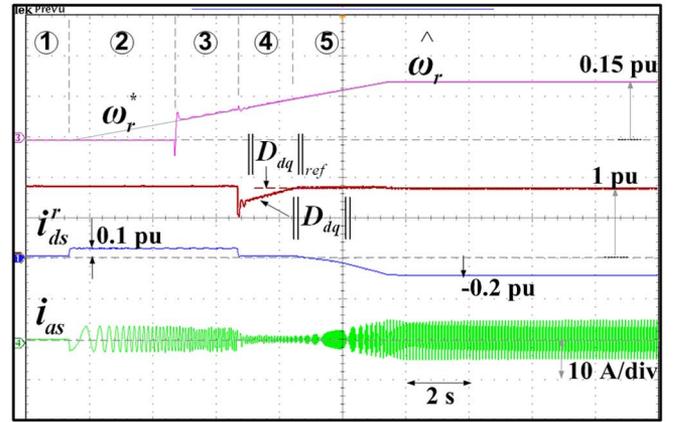
Once the state observer and tracking controller have been evaluated, the next subsection will elaborate on the performance of current regulator in estimated reference frame.

### C. Current Controller

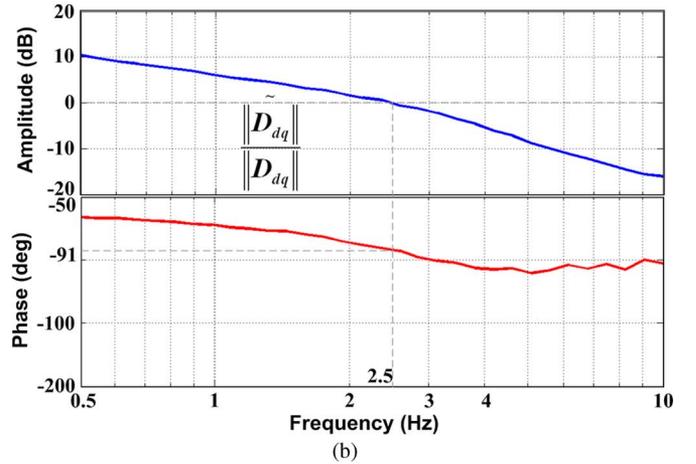
The current controller in estimated reference frame is evaluated by applying a step reference change on the  $d$ -axis. Fig. 16(a) shows the response of the motor drive, depicting a step change of 10-A peak. It can be seen that the current reaches steady state within 4 ms. The plot in Fig. 16(b) shows the current controller open-loop gain highlighting the ratio of  $d$ -axis current error to the measured  $d$ -axis current. The gain crossover frequency is 148 Hz, while the phase margin at this frequency is  $47^\circ$ . Since the machine does not have a salient rotor, the same bandwidths are applicable to both  $d$ - and  $q$ -axis current regulators. Considering the phase margin and the gain crossover frequency, the current controller open-loop bandwidth is within acceptable range in comparison to the design criteria. Then, it is essential to evaluate the speed controller response, and it will be discussed in the next subsection.

### D. Speed Controller

The dynamic requirements for fan-type applications are low, and hence, low bandwidths are usually preferred. Fig. 17(a)



(a)



(b)

Fig. 18. Experimental results. (a) Machine startup including flux-weakening operation highlighting estimated and reference speed, reference and actual maximum duty cycle, measured  $d$ -axis current, and phase current. (b) Anti-saturation flux-weakening controller open-loop gain highlighting ratio of error in magnitude of duty cycle to the actual duty cycle.

shows a speed controller response to a 75% step load change from 0 to 15 N·m. A 14% undershoot is observed as the estimated speed returns to its reference value, while the phase current changes to 10 A. Although such load conditions are unlikely in the given application, the speed regulator performance demonstrated in Fig. 17(a) shows a stable operation by applying the controller explained in Section VII-B. Fig. 17(b) shows that the gain crossover frequency is 3.6 Hz, while the phase margin is  $65^\circ$ .

### E. Antisaturation Flux-Weakening Controller

After verifying the anticipated operation of the current and speed loops, the antisaturation flux-weakening control loop was closed for its corresponding verification. The machine was operated at a dc-link voltage of 110 V in constant-torque region of operation and, then, at 100 V to allow the operation in the flux-weakening region. The reference speed was unchanged in both the operating modes.

Fig. 18(a) shows the machine startup operation including the flux-weakening region with focus on estimated speed, reference and actual maximum duty cycle, measured  $d$ -axis current, and phase current. The operation of the system is explained as

follows. After rotor position is aligned in *Region 1*, the motor starts up in *Region 2* using current vector rotation with  $d$ -axis current defined at 0.1 p.u. Observer and tracking controllers are engaged in *Region 3* when the machine passes the prespecified initial speed. With the onset of *Region 4*, the speed loop is closed; correspondingly, the  $d$ -axis current is set to zero, while the  $q$ -axis current, which is the output of the speed regulator, generates the required torque to accelerate the motor. As the speed further increases, the maximum duty-cycle vector amplitude increases linearly, which is observed at the onset of *Region 4*. As the amplitude of this duty-cycle vector reaches 1 p.u., the inverter saturates to its voltage limit of 1 p.u.; however, the speed has yet to reach the reference value. It is then when the antisaturation regulator engages and generates a negative  $d$ -axis current to weaken the flux until the speed reaches its steady-state reference value of 0.15 p.u. It should be noted that the maximum duty-cycle vector is limited to its reference value of 1 p.u. The steady-state  $d$ -axis current amplitude achieved in this case is 0.2 p.u., which has resulted in an increase in the phase current amplitude.

Fig. 18(b) shows that the gain crossover frequency is 2.5 Hz while the phase margin is  $89^\circ$ . Overall, a stable operation is observed, including the transition from constant-torque *Region 4* to the flux-weakening *Region 5*, validating the controller structure defined in Section VII-C.

## IX. CONCLUSION

This paper has presented a design methodology for the sensorless vector control of PMSM PWM motor drives in fan-type applications. Specifically, detailed derivations and design rules were given for all control loops—including antiwindup loops, verified through time-domain simulations; frequency-response analysis; and experimental results with a 7.5-kW PMSM motor drive. The proposed strategy used a two-stage approach based on a linear asymptotic state observer to estimate the machine back EMF and a novel PLL-based tracking controller used to estimate the machine speed and rotor position, achieving linear dynamics throughout the complete operating region. Vector controls were implemented over the estimation engine featuring the following: linear and decoupled dynamics, transient-performance optimized speed-loop controls, and inherent flux-weakening operation attained through an antisaturation control loop. The results presented throughout this paper validate the proposed design and control methodology.

## APPENDIX

The following are the PMSM motor-drive parameters used:

Symbol	Value
$r_s$	0.37 $\Omega$ ;
$L_s$	4.3 mH;
$\lambda_m$	0.1774 V <sub>p</sub> /rad/s;
poles ( $P$ )	8;
speed	3000 r/min;
torque	20 N · m;
power	7.5 kW;
inertia $J_m$	1.2m kg · m <sup>2</sup> .

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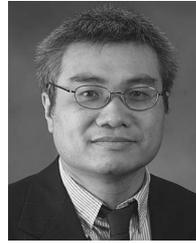


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